

Procedimentos Graficos em Calculo Integral



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Maple

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Este procedimento plota as seis regiões de integração expressas em coordenadas esféricas. As coordenadas esféricas são ρ (raio), θ (angulo longitudinal; i.e., ângulo feito por $(x,y,0)$ e eixo x), e ϕ (ângulo latitudinal; i.e., ângulo feito por (x,y,z) e o eixo positivo de z).

Este procedimento plota a fronteira da região no espaço quando descrita em coordenadas esféricas (ρ, θ, ϕ) , determinada pelas desigualdades

$$\rho = f(\theta, \phi) .. g(\theta, \phi) , \theta = h(\phi) .. k(\phi) , \phi = a .. b ,$$

Isto é, ρ varia entre $f(\theta, \phi)$ e $g(\theta, \phi)$

e θ varia entre $h(\phi)$ e $k(\phi)$

e ϕ varia entre a e b .

Sintaxe: `dptdphiplot($\rho = f(\theta, \phi) .. g(\theta, \phi)$, $\theta = h(\phi) .. k(\phi)$, $\phi = a .. b$,opts)`

Os cinco procedimentos análogos são:

`dpdhidtplot,`

`dtdpdphiplot,`

`dtdphidpplot,`

`dphidtdpplot,`

`dphidpdtplot,`

todos com sintaxes análogas.

Execute o procedimento e faça os exemplos.

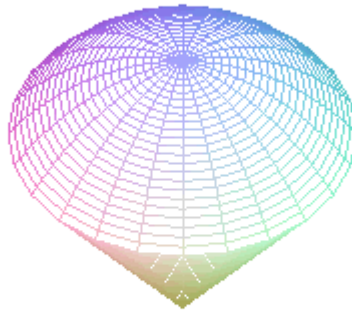
O Procedimento (execute-o)

Exemplos

Exemplos # dpdtdphiplot

```
> dpdphidtpplot(rho=0..2,phi=0..Pi/4,theta=0..2*Pi, title=`exemplo`);
```

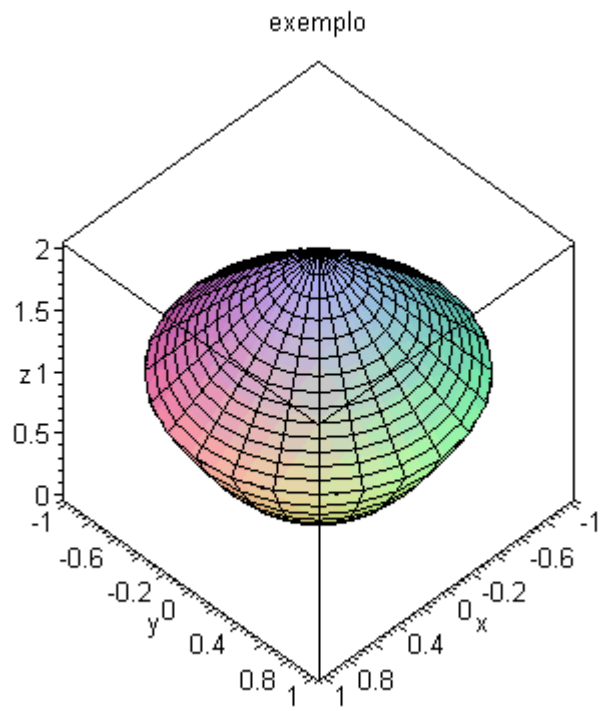
exemplo



```
> P1:=dpdtdphiplot(rho=sec(phi)..2/(cos(phi)+sin(phi)),theta=0..2*Pi,phi=0..Pi/4):
```

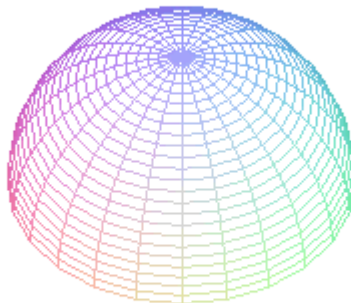
```
> P2:=dpdtdphiplot(rho=0..cot(phi)*csc(phi),theta=0..2*Pi,phi=Pi/4..Pi/2):
```

```
> plots[display3d]({P1,P2},style=wireframe,title=`exemplo`);
```

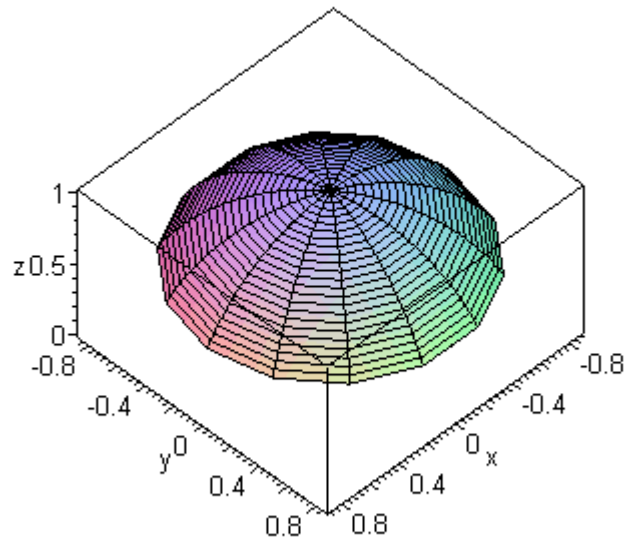


> **dphidplot(rho=0.2*cos(phi),phi=0..Pi/4,theta=0.2*Pi, title=`18.7-5`);**

18.7-5

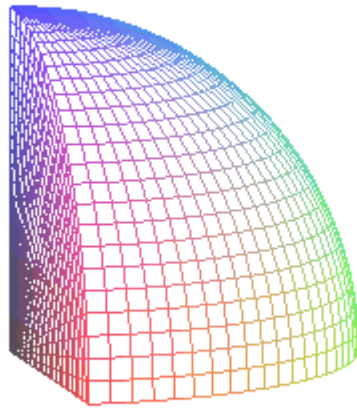


> **dphidplot(phi=0..Pi/3,rho=0..1,theta=0.2*Pi);**



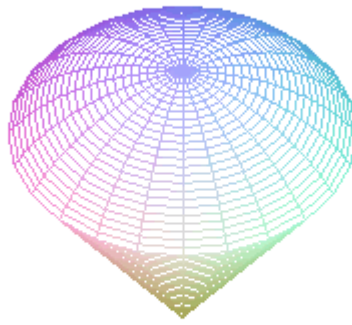
> `dphidplot(phi=0..Pi/2,rho=0..1,theta=0..Pi/2,title= `esfera no primeiro octante`);`

esfera no primeiro octante



> `dphidplot(rho=0..2*cos(phi),phi=0..Pi/6,theta=0..2*Pi, title=`cone de sorvete`);`

cone de sorvete



>

O Procedimento (execute-o)

#1. d(rho)d(theta)d(phi)

- > **dpdtdphiplot:= proc()**
- > **local surface, f, f1, g, g1, h, h1, k, k1, a, b, p1, q1, t1, phi1, u,**
- > **v, uloc, uloc1, uloc2, vloc, wloc, xloc, yloc, zloc, i, opt_seq,**
- > **pbound, tbound, phibound;**
- > **if nargs < 3 then**
- > **ERROR(`there must be at least three arguments`) fi;**
- > **pbound:=args[1];**
- > **tbound:=args[2];**
- > **phibound:=args[3];**
- > **a:=op(1, rhs(phibound));**
- > **b:=op(2, rhs(phibound));**
- > **if not type (phibound, string = range) or not (op(1, pbound) = 'rho') or not (op(1, tbound) = 'theta') or not (op(1, phibound) = 'phi')**
- > **or not type (evalf(a), numeric) or not type (evalf(b), numeric) then**
- > **ERROR(`input expression is not of dpdtdphi type`) fi;**
- > **f:=op(1, rhs(pbound));**
- > **g:=op(2, rhs(pbound));**
- > **h:=op(1, rhs(tbound));**
- > **k:=op(2, rhs(tbound));**
- > **p1:=lhs(pbound);**
- > **t1:=lhs(tbound);**
- > **phi1:=lhs(phibound);**
- > **f1:=unapply(f,(t1,phi1));**
- > **g1:=unapply(g,(t1,phi1));**

```

> h1:=unapply(h,phi1);
> k1:=unapply(k,phi1);
> uloc:=u*b+(1-u)*a;
> uloc1:=u*h1(a)+(1-u)*k1(a);
> uloc2:=u*h1(b)+(1-u)*k1(b);
> vloc:=v*k1(uloc)+(1-v)*h1(uloc);
> wloc:=v*f1(h1(uloc),uloc)+(1-v)*g1(h1(uloc),uloc);
> xloc:=v*f1(k1(uloc),uloc)+(1-v)*g1(k1(uloc),uloc);
> yloc:=v*f1(uloc1,a)+(1-v)*g1(uloc1,a);
> zloc:=v*f1(uloc2,b)+(1-v)*g1(uloc2,b);
> surface:={f1(vloc,uloc),vloc,uloc],[g1(vloc,uloc),vloc,uloc],
> [wloc,h1(uloc),uloc], [xloc,k1(uloc),uloc],[yloc,uloc1,a],[zloc,uloc2,b]};
> if nargs =3 then
> q1:=plots[sphereplot](surface, u=0..1, v=0..1, axes=BOXED, grid
> =[15,25],style=PATCH, scaling=CONSTRAINED); fi;
> if nargs > 3 then
> opt_seq:=seq(args[i],`i`=4..nargs);
> q1:=plots[sphereplot](surface, u=0..1, v=0..1),opt_seq; fi;
> plots[display3d](q1);
> end:

```

#2. $d(\rho)d(\phi)d(\theta)$

```

> dphidplot:= proc()
> local surface, f, f1, g, g1, h, h1, k, k1, a, b, p1, q1, t1, phi1, u,
> v, uloc, uloc1, uloc2, vloc, wloc, xloc, yloc, zloc, i, opt_seq,
> pbound, tbound, phibound;
> if nargs < 3 then

```

```

> ERROR(`there must be at least three arguments`) fi;
> pbound:=args[1];
> phibound:=args[2];
> tbound:=args[3];
> a:=op(1, rhs(tbound));
> b:=op(2, rhs(tbound));
> if not type (phibound, string = range) or not (op(1, pbound) = 'rho') or not (op(1, tbound) = 'theta') or not (op(1, phibound) = 'phi')
> or not type (evalf(a), numeric) or not type (evalf(b), numeric) then
> ERROR(`input expression is not of dpdphidt type` ) fi;
> f:=op(1, rhs(pbound));
> g:=op(2, rhs(pbound));
> h:=op(1, rhs(phibound));
> k:=op(2, rhs(phibound));
> p1:=lhs(pbound);
> t1:=lhs(tbound);
> phi1:=lhs(phibound);
> f1:=unapply(f,(phi1,t1));
> g1:=unapply(g,(phi1,t1));
> h1:=unapply(h,t1);
> k1:=unapply(k,t1);
> uloc:=u*b+(1-u)*a;
> uloc1:=u*h1(a)+(1-u)*k1(a);
> uloc2:=u*h1(b)+(1-u)*k1(b);
> vloc:=v*k1(uloc)+(1-v)*h1(uloc);
> wloc:=v*f1(h1(uloc),uloc)+(1-v)*g1(h1(uloc),uloc);
> xloc:=v*f1(k1(uloc),uloc)+(1-v)*g1(k1(uloc),uloc);

```



```

> yloc:=v*f1(uloc1,a)+(1-v)*g1(uloc1,a);
> zloc:=v*f1(uloc2,b)+(1-v)*g1(uloc2,b);
> surface:={f1(vloc,uloc),uloc,vloc],[g1(vloc,uloc),uloc,vloc],
> [wloc,uloc,h1(uloc)], [xloc,uloc,k1(uloc)],[yloc,a,uloc1],[zloc,b,uloc2]};
> if nargs =3 then
> q1:=plots[sphereplot](surface, u=0..1, v=0..1, axes=BOXED, grid
> =[15,25],style=PATCH, scaling=CONSTRAINED); fi;
> if nargs > 3 then
> opt_seq:=seq(args[i], i`=4..nargs);
> q1:=plots[sphereplot](surface, u=0..1, v=0..1),opt_seq; fi;
> plots[display3d](q1);
> end:

```

#3. d(theta)d(phi)d(rho)

```

> dtdphidpplot:= proc()
> local surface, f, f1, g, g1, h, h1, k, k1, a, b, p1, q1, t1, phi1, u,
> v, uloc, uloc1, uloc2, vloc, wloc, xloc, yloc, zloc, i, opt_seq,
> pbound, tbound, phibound;
> if nargs < 3 then
> ERROR(`there must be at least three arguments`) fi;
> tbound:=args[1];
> phibound:=args[2];
> pbound:=args[3];
> a:=op(1, rhs(pbound));
> b:=op(2, rhs(pbound));
> if not type (phibound, string = range) or not (op(1, pbound) = 'rho')or not (op(1, tbound) =
'theta') or not (op(1, phibound) = 'phi')
> or not type (evalf(a),numeric) or not type(evalf(b), numeric) then

```

```

> ERROR( input expression is not of dtdphidp type` ) fi;
> f:=op(1, rhs(tbound));
> g:=op(2, rhs(tbound));
> h:=op(1, rhs(phibound));
> k:=op(2, rhs(phibound));
> p1:=lhs(pbound);
> t1:=lhs(tbound);
> phi1:=lhs(phibound);
> f1:=unapply(f,(phi1,p1));
> g1:=unapply(g,(phi1,p1));
> h1:=unapply(h,p1);
> k1:=unapply(k,p1);
> uloc:=u*b+(1-u)*a;
> uloc1:=u*h1(a)+(1-u)*k1(a);
> uloc2:=u*h1(b)+(1-u)*k1(b);
> vloc:=v*k1(uloc)+(1-v)*h1(uloc);
> wloc:=v*f1(h1(uloc),uloc)+(1-v)*g1(h1(uloc),uloc);
> xloc:=v*f1(k1(uloc),uloc)+(1-v)*g1(k1(uloc),uloc);
> yloc:=v*f1(uloc1,a)+(1-v)*g1(uloc1,a);
> zloc:=v*f1(uloc2,b)+(1-v)*g1(uloc2,b);
> surface:={[uloc,f1(vloc,uloc),vloc],[uloc,g1(vloc,uloc),vloc],
> [uloc,wloc,h1(uloc)], [uloc,xloc,k1(uloc)],[a,yloc,uloc1],[b,zloc,uloc2]};
> if nargs =3 then
> q1:=plots[sphereplot](surface, u=0..1, v=0..1, axes=BOXED, grid
> =[15,25],style=PATCH, scaling=CONSTRAINED); fi;
> if nargs > 3 then

```

```

> opt_seq:=seq(args[i], i`=4..nargs);
> q1:=plots[sphereplot](surface, u=0..1, v=0..1),opt_seq; fi;
> plots[display3d](q1);
> end:

```

#4. d(phi)d(theta)d(rho)

```

> dphidtdpplot:= proc()
> local surface, f, f1, g, g1, h, h1, k, k1, a, b, p1, q1, t1, phi1, u,
> v, uloc, uloc1, uloc2, vloc, wloc, xloc, yloc, zloc, i, opt_seq,
> pbound, tbound, phibound;
> if nargs < 3 then
> ERROR(`there must be at least three arguments`) fi;
> phibound:=args[1];
> tbound:=args[2];
> pbound:=args[3];
> a:=op(1, rhs(pbound));
> b:=op(2, rhs(pbound));
> if not type (phibound, string = range) or not (op(1, pbound) = 'rho') or not (op(1, tbound) =
'theta') or not (op(1, phibound) = 'phi')
> or not type (evalf(a), numeric) or not type(evalf(b), numeric) then
> ERROR(`input expression is not of dphidtdp type`) fi;
> f:=op(1, rhs(phibound));
> g:=op(2, rhs(phibound));
> h:=op(1, rhs(tbound));
> k:=op(2, rhs(tbound));
> p1:=lhs(pbound);
> t1:=lhs(tbound);
> phi1:=lhs(phibound);

```

```

> f1:=unapply(f,(t1,p1));
> g1:=unapply(g,(t1,p1));
> h1:=unapply(h,p1);
> k1:=unapply(k,p1);
> uloc:=u*b+(1-u)*a;
> uloc1:=u*h1(a)+(1-u)*k1(a);
> uloc2:=u*h1(b)+(1-u)*k1(b);
> vloc:=v*k1(uloc)+(1-v)*h1(uloc);
> wloc:=v*f1(h1(uloc),uloc)+(1-v)*g1(h1(uloc),uloc);
> xloc:=v*f1(k1(uloc),uloc)+(1-v)*g1(k1(uloc),uloc);
> yloc:=v*f1(uloc1,a)+(1-v)*g1(uloc1,a);
> zloc:=v*f1(uloc2,b)+(1-v)*g1(uloc2,b);
> surface:={[uloc,vloc,f1(vloc,uloc)],[uloc,vloc,g1(vloc,uloc)],
> [uloc,h1(uloc),wloc], [uloc,k1(uloc),xloc],[a,uloc1,yloc],[b,uloc2,zloc]};
> if nargs =3 then
> q1:=plots[sphereplot](surface, u=0..1, v=0..1, axes=BOXED, grid
> =[15,25],style=PATCH, scaling=CONSTRAINED); fi;
> if nargs > 3 then
> opt_seq:=seq(args[i], `i`=4..nargs);
> q1:=plots[sphereplot](surface, u=0..1, v=0..1),opt_seq; fi;
> plots[display3d](q1);
> end:

```

#5. d(theta)d(rho)d(phi)

```

> dtdpdphiplot:= proc()
> local surface, f, f1, g, g1, h, h1, k, k1, a, b, p1, q1, t1, phi1, u,
> v, uloc, uloc1, uloc2, vloc, wloc, xloc, yloc, zloc, i, opt_seq,

```

```

> pbound, tbound, phibound;
> if nargs < 3 then
> ERROR(`there must be at least three arguments`) fi;
> tbound:=args[1];
> pbound:=args[2];
> phibound:=args[3];
> a:=op(1, rhs(pbound));
> b:=op(2, rhs(pbound));
> if not type (phibound, string = range) or not (op(1, pbound) = 'rho') or not (op(1, tbound) = 'theta') or not (op(1, phibound) = 'phi')
> or not type (evalf(a),numeric) or not type(evalf(b), numeric) then
> ERROR(`input expression is not of dtdpdphi type`) fi;
> f:=op(1, rhs(tbound));
> g:=op(2, rhs(tbound));
> h:=op(1, rhs(phibound));
> k:=op(2, rhs(phibound));
> p1:=lhs(pbound);
> t1:=lhs(tbound);
> phi1:=lhs(phibound);
> f1:=unapply(f,(p1,phi1));
> g1:=unapply(g,(p1,phi1));
> h1:=unapply(h,p1);
> k1:=unapply(k,p1);
> uloc:=u*b+(1-u)*a;
> uloc1:=u*h1(a)+(1-u)*k1(a);
> uloc2:=u*h1(b)+(1-u)*k1(b);
> vloc:=v*k1(uloc)+(1-v)*h1(uloc);

```

```

> wloc:=v*f1(h1(u loc),u loc)+(1-v)*g1(h1(u loc),u loc);
> xloc:=v*f1(k1(u loc),u loc)+(1-v)*g1(k1(u loc),u loc);
> yloc:=v*f1(u loc1,a)+(1-v)*g1(u loc1,a);
> zloc:=v*f1(u loc2,b)+(1-v)*g1(u loc2,b);
> surface:={vloc,f1(vloc,u loc),u loc},[vloc,g1(vloc,u loc),u loc],
> [h1(u loc),wloc,u loc], [k1(u loc),xloc,u loc],[u loc1,yloc,a],[u loc2,zloc,b]];
> if nargs =3 then
> q1:=plots[sphereplot](surface, u=0..1, v=0..1, axes=BOXED, grid
> =[15,25],style=PATCH, scaling=CONSTRAINED); fi;
> if nargs > 3 then
> opt_seq:=seq(args[i], i`=4..nargs);
> q1:=plots[sphereplot](surface, u=0..1, v=0..1),opt_seq; fi;
> plots[display3d](q1);
> end:

```

#6. $d(\phi)d(\rho)d(\theta)$

```

> dphidpdtplot:= proc()
> local surface, f, f1, g, g1, h, h1, k, k1, a, b, p1, q1, t1, phi1, u,
> v, u loc, u loc1, u loc2, vloc, wloc, xloc, yloc, zloc, i, opt_seq,
> pbound, tbound, phibound;
> if nargs < 3 then
> ERROR(`there must be at least three arguments`) fi;
> phibound:=args[1];
> pbound:=args[2];
> tbound:=args[3];
> a:=op(1, rhs(tbound));
> b:=op(2, rhs(tbound));

```

```

> if not type (phibound, string = range) or not (op(1, pbound) = 'rho') or not (op(1, tbound) =
'theta') or not (op(1, phibound) = 'phi')
> or not type (evalf(a), numeric) or not type (evalf(b), numeric) then
> ERROR(`input expression is not of dphidpdt type`) fi;
> f:=op(1, rhs(phibound));
> g:=op(2, rhs(phibound));
> h:=op(1, rhs(pbound));
> k:=op(2, rhs(pbound));
> p1:=lhs(pbound);
> t1:=lhs(tbound);
> phi1:=lhs(phibound);
> f1:=unapply(f,(p1,t1));
> g1:=unapply(g,(p1,t1));
> h1:=unapply(h,t1);
> k1:=unapply(k,t1);
> uloc:=u*b+(1-u)*a;
> uloc1:=u*h1(a)+(1-u)*k1(a);
> uloc2:=u*h1(b)+(1-u)*k1(b);
> vloc:=v*k1(uloc)+(1-v)*h1(uloc);
> wloc:=v*f1(h1(uloc),uloc)+(1-v)*g1(h1(uloc),uloc);
> xloc:=v*f1(k1(uloc),uloc)+(1-v)*g1(k1(uloc),uloc);
> yloc:=v*f1(uloc1,a)+(1-v)*g1(uloc1,a);
> zloc:=v*f1(uloc2,b)+(1-v)*g1(uloc2,b);
> surface:=[vloc,uloc,f1(vloc,uloc)],[vloc,uloc,g1(vloc,uloc)],
> [h1(uloc),uloc,wloc], [k1(uloc),uloc,xloc],[uloc1,a,yloc],[uloc2,b,zloc]];
> if nargs =3 then
> q1:=plots[sphereplot](surface, u=0..1, v=0..1, axes=BOXED, grid

```

```
> =[15,25],style=PATCH, scaling=CONSTRAINED); fi;  
> if nargs > 3 then  
> opt_seq:=seq(args[i], `i`=4..nargs);  
> q1:=plots[sphereplot](surface, u=0..1, v=0..1),opt_seq; fi;  
> plots[display3d](q1);  
> end;
```