

# Procedimentos Graficos em Calculo Integral



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**Maple**

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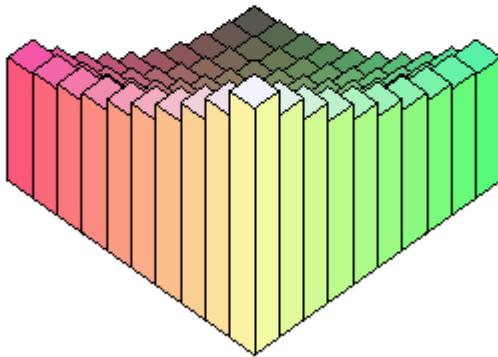
Este procedimento plota a soma de Riemann em 3 dimensões. Você pode conjugar o gráfico da função com a soma de Riemann em 3 dimensoes.

[Execute o procedimento e faça os exemplos.](#)

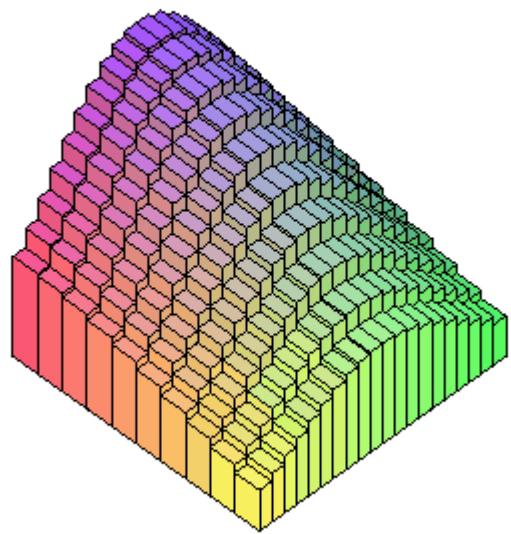
## O Procedimento (execute-o)

### Exemplos

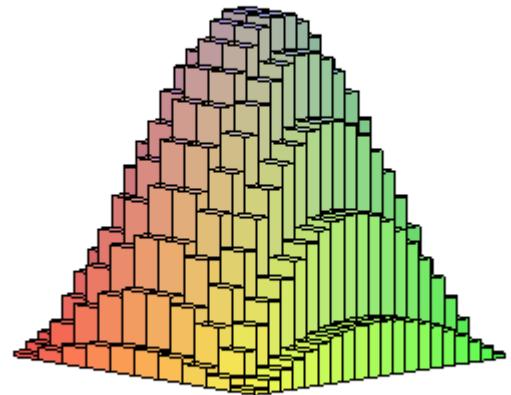
> **riemann3d(u^2+v^2,u=0..1,v=0..1);**



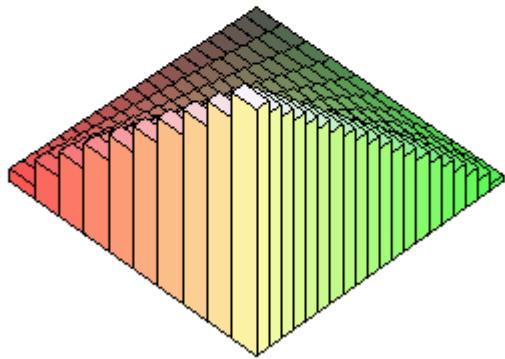
> **riemann3d(exp(-u^2-v^2),u=-1..1,v=0..1,grid=[20,10]);**



```
> riemann3d(sin(x)*sin(y),x=0..Pi,y=0..Pi,grid=[20,10]);
```

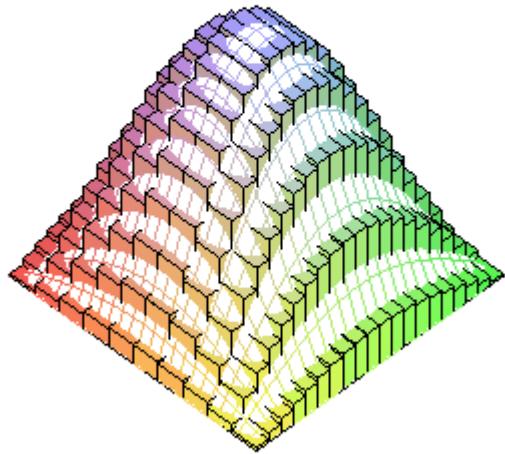


```
> riemann3d(x*y,x=0..4,y=0..4,grid=[20,10]);
```



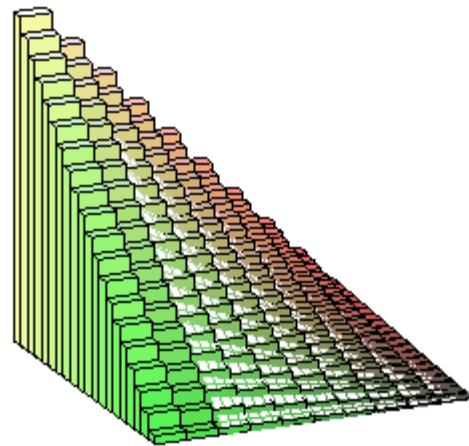
No próximo exemplo vamos plotar uma superfície e sob ela os paralelepípedos que aproximam o seu volume.

```
> with(plots):  
> p1:=plot3d(sin(x)*sin(y),x=0..Pi,y=0..Pi):  
> p2:=riemann3d(sin(x)*sin(y),x=0..Pi,y=0..Pi,grid=[20,10]):  
> plots[display3d]({p1,p2});
```



Outro exemplo uma superfície e sob ela os paralelepípedos que aproximam o seu volume.

```
> q1:=riemann3d(x*y,x=0..4,y=0..4,grid=[20,10]):  
> q2:=plot3d(x*y,x=0..Pi,y=0..Pi):  
> plots[display3d]({q1,q2});
```



>



## O Procedimento (execute-o)

```
> riemann3d := proc ()  
> local f,r1,r2,a,b,c,d,v1,v2,n,m,i,j,L,step1,step2,v;  
> r1 := args[2];  
> r2 := args[3];  
> a := convert(convert(r1,list)[2],list)[1];  
> b := convert(convert(r1,list)[2],list)[2];  
> c := convert(convert(r2,list)[2],list)[1];  
> d := convert(convert(r2,list)[2],list)[2];  
> v1 := convert(r1,list)[1];  
> v2 := convert(r2,list)[1];  
> f := unapply(args[1],v1,v2);  
> # default grid  
> n := 10;  
> m := 10;  
> for i from 3 to nargs  
> do  
> if type(args[i],`=)` then  
> if convert(args[i],list)[1]=grid then  
> n := convert(args[i],list)[2][1];  
> m := convert(args[i],list)[2][2];  
> fi;  
> fi;  
> od;  
> step1 := (b-a)/n;  
> step2 := (d-c)/m;
```

```

> L := plot3d([0,0,0],r1,r2):
> for j from 0 to m-1 do
> for i from 0 to n-1 do
> v := f(a+i*step1+step1/2,c+j*step2+step2/2);
> L := L,plots[polygonplot3d]([[a+step1*i,c+step2*j,0],
> [a+step1+step1*i,c+step2*j,0],[a+step1+step1*i,c+step2*j,v],
> [a+step1*i,c+step2*j,v]],style=patch):
> L := L,plots[polygonplot3d]([[a+step1*i,c+step2*j,0],
> [a+step1+step1*i,c+step2+step2*j,0],[a+step1+step1*i,c+step2+step2*j,v],
> [a+step1*i,c+step2+step2*j,v]],style=patch):
> L := L,plots[polygonplot3d]([[a+step1+step1*i,c+step2*j,0],
> [a+step1+step1*i,c+step2+step2*j,0],[a+step1+step1*i,c+step2+step2*j,v],
> [a+step1+step1*i,c+step2+step2*j,v]],style=patch):
> L := L,plots[polygonplot3d]([[a+step1+step1*i,c+step2+step2*j,0],
> [a+step1+step1*i,c+step2+step2*j,0],[a+step1+step1*i,c+step2+step2*j,v],
> [a+step1+step1*i,c+step2+step2*j,v]],style=patch):
> L := L,plots[polygonplot3d]([[a+step1+step1*i,c+step2+step2*j,0],
> [a+step1+step1*i,c+step2+step2*j,0],[a+step1+step1*i,c+step2+step2*j,v],
> [a+step1+step1*i,c+step2+step2*j,v]],style=patch):
> L := L,plots[polygonplot3d]([[a+step1+step1*i,c+step2+step2*j,0],
> [a+step1+step1*i,c+step2+step2*j,0],[a+step1+step1*i,c+step2+step2*j,v],
> [a+step1+step1*i,c+step2+step2*j,v]],style=patch):
> od;
> od;
> plots[display3d](L);
> end:
```